## HANDS-ON, MINDS-ON MATH - AN OFFERING OF HOMEGROWN MATH PROJECTS AND ACTIVITIES

MARCH 1, 2014
HTTP://MHINES.EDUBLOGS.ORG HTTP://MIDPAC.EDU/
@MHINES TWITTER


## GOAL

- Activities and Projects
- Strategies and Apps
- Guide sheets
- Assessment rubrics
- Student samples
- Common Core standards mapping
- Time Frame: range 90 mins to 8 class periods



## A BRIEF HISTORY

- STEM Teacher for 30 years
- MEd Edtech '97, finishing PhD EdTech ('14)
- Technology Director 17 years
- HSTE Board, SEEOS Board
- Father of Aukai, 16 and Ka'io 11
- SoTF and HELS planning
- Kupu Hou Academy co-creator
- Modeling Physics (ASU)


## About MPX

MPX Program is an innovative, interdisciplinary program featuring a project-based curriculum as the primary focus of student work. This curriculum encourages students to synthesize their knowledge of Language Arts, Social Studies, Science, and Engineering through participation in collaborative "real world problem solving" setting. This school year we have projects addressing sustainability including auditing the energy use of each building on this campus that will be used to address the school's carbon footprint, and designing and constructing urban garden systems that will be used to grow produce for a cook-off competition.

On the right side of this page, you see a series of links to other activities we have done as well as links to blogs that give you a up-to-date view of the work our leaders and learners are doing - challenges and successes, their reflections about their work and the process involved in rolling up our sleeves and trying to do authentic problem-solving.

We hope you will take time to explore the activities our learners have been immersed in. If you have an interest in being involved with our program as a resource, or have questions, please contact mpx@midpac.edu

Imual (onward!)

MID-PACIFIC INSTITUTE EXPLORATORY NEWS

## Nov On Math, Modeling and Applied learning

## Explore MPX

- MPX Home
- More about MPX
- MPX Frequently Asked Questions
- An Overview of MPX [.pdf]


## MPX Teacher Blogs

© Heather Calabro's MPX 9 Humanities Blog
(-) Mark Hines' MPX 10 STEM blog
(-) Gregg Kaneko's MPX 9 STEM blog

- Laura Davis' MPX 10 Humanities blog


## Videos/Documents

- MPX by MPX'ers
(-) Kolea Farms Field Trip
(-) Visual Mapping
(-) What is MPX? In student voice from their presentations of learning Fall 2011


## MID-PACIFIC EXPLORATORY

- Started 2010
- Project/Problem Based
- Integrated Math/Science/Lang Arts/Social Studies/Technology
- 9th Grade: Geometry/Biology 10th Grade: Algebra 2/Physics
- After 10 th, students either go Precal or Math Studies

- Typical week blocks: $1 \times 45,2 \times 90$


## APPS, APPS, APPS

Analysis

- sketchup
- Math Flyer
- geogebra
- sketch explorer
- wolfram alpha
- showme
- explain everything
- taptap blocks
- geometry pad
- Skitch
- and many more


## CRITIQUING AND FEEDBACK

THE VALUE OF CONVERSATION AND ITERATION


## AUSTIN'S BUTTERFLY

HTTP://VIMEO.COM/38247060
FROM RON BERGER, EXPEDITIONARY
LEARNING


E Austin's Butterfly: Building Excellence in Student Work - Models, Critique, and Descriptive Feedback

## "ASSESSMENT IN THE SERVICE OF LEARNING"



## LIGHT INTENSITY

- HSF-IF.B. $4 \& 5$ INTERPRET FUNCTIONS THAT ARISE IN APPLICATIONS IN TERMS OF THE CONTEXT
- HSF-BF.A. 1 BUILD A FUNCTION THAT MODELS A RELATIONSHIP BETWEEN TWO QUANTITIES
- HSF-BF.B. 4 BUILD NEW FUNCTIONS FROM EXISTING FUNCTIONS




## Activity - Light Intensity

Question: What happens to the intensity of light as we move further from the source?
Introduction: While we have been doing our lighting measurements, you may have noticed that light as it moves from the source does not stay the same intensity as you move away. The goal of this activity, is to understand the relationship that exists between a light source and its intensity as we move away from it.

## Background Information:

We will look at a few examples in class of how light spreads out as we move away from it - here a few pictorial examples of this phenomena:
http://moblog.net/media/j/x///jxlatoca/6-artificial-light-project-55-light-intensity-2.jpg
http://www.sciencebuddies.org/science-fair-projects/project ideas/Elec img052.jpg
http://www.expertsmind.com/CMSImages/26 measuer\%20by\%20light\%20inten.jpg

## Experiment and Analysis:

Using your light meter, and keeping in mind that in good science experiments we want to have at least six data points so that we can correctly determine the mathematical relationship between the dependent and independent variable, measure light intensity between the ceiling and the floor in our classroom. As accurately as possible, measure the distance at each point of measurement from the light source. Try to locate the sensor directly under the center of the light that you are measuring from.

Once you have your data, use the iPad app Graphical Analysis to plot the data, and determine the best fit curve through that data to come up with a mathematical model.

## Writeup

You should submit a document that has your graph, data table and a discussion of the data and mathematical model you have determined fits this phenomena. submit that document as a PDF into this week's drop folder.

Common Core Standards Addressed:
CCSS.Math.Content.HSF-LE.A. 1 Distinguish between situations that can be modeled with linear functions and with exponential functions
CCSS.Math.Content.HSF-LE.A.1c Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another. CCSS.Math.Content.HSF-LE.A. 2 Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).

Data Table:
Averages

|  | Distance (cm) | Light Intensity <br> (ux) |
| :---: | :---: | :---: |
| 1 |  |  |
| 2 | 50 | 3,516 |
| 3 | 100 | 1,322 |
| 4 | 150 | 766 |
| 5 | 200 | 696 |
| 6 | 250 | 600 |
| 7 | 300 | 380 |

Graph


In order to get the light intensity you need to divide 7.42 million divided by the distance squared plus $b$ which is 443.6 . This relationship shows that the light intensity decreases the further you get. This is an inverse squared relationship.

## LINEARIZE THAT!

- UNDERSTAND THE CONCEPT OF A FUNCTION AND USE FUNCTION NOTATION (FIF 1,2)
- CREATE EQUATIONS THAT DESCRIBE NUMBERS OR RELATIONSHIPS (ACED 2)
- INTERPRET FUNCTIONS THAT ARISE IN APPLICATIONS IN TERMS OF CONTEXT (FIF 4, 5, 6)
- BUILD A FUNCTION THAT MODELS A RELATIONSHIP BETWEEN TWO QUANTITIES (FBF 1)


Mathematical Models and Modeling Functions
Goal: To design and practice the common core standards around linear model functions
Step 1. Define and design an experiment that you can conduct with existing classroom equipment that will generate a set of at at least $\mathbf{6}$ data pairs to examine the relationship between two variables of your choosing.
Your goal should be for this data to test a hypothesis that the relation is linear. You must get permission for the teacher to move forward to step 2. You must define:

- your purpose
- your independent and dependent variables
- your anticipated domain and range
- your rationale for why you expect a linear relationship
- your apparatus and procedure

Step 2: Conduct the experiment. Make sure to run AT LEAST 3 trials to minimize error.
Step 3: For your submitted report, you must complete the EVALUATION section of our standard lab report:

- a table of calculated values
- a graph that includes appropriate axes and labels as well as attempts to linearize your data
- a statement of the relationship
- a mathematical model of the data, including slope and intercept with correct units.
(This should be in slope intercept form)
- a brief discussion of the results and any divergent issues

Common Core Standards Addressed:

- Understand the concept of a function and use function notation (F-IF 1,2) Create equations that describe numbers or relationships (A-CED 2)
- Interpret functions that arise in applications in terms of context (F-IF 4, 5, 6) Analyze functions using different representations. (F-IF 7, 8, 9)
- Build a function that models a relationship between two quantities (F-BF 1)

MPI Math Core Concepts Addressed:
Relation Properties, Domain and Range, Functions Properties, Function Notation Direct Variation, Slope, Slope-Intercept form, Graphing Lines


Purpose: To determine what the rate a slinky falls from different numbers of steps Independent variable: stairs
Dependent variable: time
Anticipated domain and range: 1-6

I think this will be linear because I think the slinky will fall slower from a higher number of steps but will travel faster from a lower number of steps. This will make a linear line.

Apparatus:


Procedure:

1. Set up slinky at top of step
2. Get timer ready
3. Using your hand, grab the top of the slinky an push it forward
4. Let the slinky fall down the steps
5. Stop timer when slinky stops
6. Repeat for each step

| Data Table |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
|  | Step <br> 1(sec) | Step 2 <br> (sec) | Step 3 <br> (sec) | Step 4 <br> (sec) | Step 5 <br> (sec) |
| Trial 1 | 2.9 | 3.5 | 3.5 | 3.0 | 4 |
| Trial 2 | 2.0 | 2.7 | 2.9 | 3.3 | 4 |
| Trial 3 | 2.8 | 3.7 | 5.7 | 3.6 | 4 |


|  | Steps (\#) | Time (sec) |
| :---: | :---: | :---: |
| 1 | 1 | 2.5 |
| 2 | 2 | 3.3 |
| 3 | 3 | 4 |
| 4 | 4 | 3.3 |
| 5 | 5 | 4.6 |
| 6 | 6 | 5.8 |

## Graph



## $\mathrm{S}=.6 \mathrm{sec}+1.947$ steps

This graph shows that the line is not very linear. I think it wasn't as linear because the experiment was flawed in that the slinky did not fall correctly and wasn't very reliable. You can see this in the difference in data in terms of the fourth step average drops very low. I think that I would change that if I were to do the experiment again and try and fix the slinky. effect the height of the bounce

| Height (cm) | Average (cm) |
| :--- | ---: |
| 50 |  |
| 100 | 26.6 |
| 150 | 54 |
| 200 | 76 |
| 250 | 100 |
| 300 | 117.3 |


$\mathrm{BH}(\mathrm{DH})=.45(\mathrm{DH})+4.94 \mathrm{~cm}$

## Evaluation:

The relationship of this graph is that for every 50 cm you add as the starting point, the bounce height of the ball increase about $20-30 \mathrm{~cm}$ each time. The relationship between the bounce height and starting height is that if starting ball height increases then the bounce height will increase as well. The equation to represent this graph would be $\mathrm{BH}(\mathrm{DH})=.45(\mathrm{DH})+4.94 \mathrm{~cm}$. Where H is the height, . 45 is the slope, (DH) is rise over run and 4.94 cm is the $y$-intercept.

## THE WORM BIN

- HSG-GMD.A. $1 \& 2 \& 3$ APPLY GEOMETRIC CONCEPTS IN MODELING SITUATIONS
- HSG-GMD.A. $1 \& 3$ EXPLAIN VOLUME FORMULAS AND USE THEM TO SOLVE PROBLEMS
- HSG-GMD.B. 4 VISUALIZE RELATIONSHIPS BETWEEN 2-D AND 3-D OBJECTS



Before we get to the BIG PROJECT, we need to go through the design/build process with something simpler.

Objective: Design and build a functioning worm composting bin.
Description: Groups will be given limited wood choices and supplies (to be defined later) and will design and build a miniature, FUNCTIONING worm compost bin.

Through the process you will be required to show different geometric concepts. -triangles
-side relationships
-angle relationships
-properties of triangles
-lines
-properties of parallel lines
-congruency of angles with parallel lines
And biological concepts
-systems
-composting
-microorganisms
Process: This project will happen through a series of steps.
Steps $1 \& 2$ will be on a pages document. Use pictures and diagrams as necessary.

1. Define the problem: Why composting? Why is it important for the environment and sustainability?
2. Research
a. Understanding of worm composting process
i. Biological standpoint
ii. Practical standpoint
b. Understanding of a properly functioning worm bin
i. What are the essential parts?
3. Design: Using the restraints in materials design a miniature worm composting bin.
a. List of materials
b. SCALE drawing of all parts needed to construct the bin
i. 3 different views
ii. Dimensions
iii. Dimensions of all parts
4. Build model: Using cardboard construct a rough model of your worm bin.
5. Edit design: Make any changes necessary to design.
6. BUILD FINAL PRODUCT.

| WORM BIN RUBRIC |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Category | Mastery | Developing | Lacking? |  |
| PRODUCT 10 pts |  |  |  |  |
| Final Product: <br> Completed Worm Bin | Group completes a fully <br> functioning worm bin that <br> fits project restraints | Does not fit restraints <br> or may not be complete | Major completion <br> issues. |  |
| Poster 10 pts |  |  |  |  |
| Pictures/ <br> documentation of <br> Progress <br> $\mathbf{2 ~ p t s ~}$ |  |  |  |  |
| Summary of Process <br> $\mathbf{2 ~ p t s ~}$ | Students clearly show <br> geometry and biology <br> concepts learned through <br> the project. These <br> concepts are properly <br> displayed in on their <br> poster. | Students showed <br> learning of geometry <br> and biology concepts. <br> Not as many concepts <br> or lacks some depth <br> from mastery. | Students either did not <br> clearly show learning or <br> there was too few <br> evidences of learning. |  |
| Evidence of Learning <br> $\mathbf{3 ~ p t s ~}$ | Students exhibited deep <br> thought and reflection of <br> the PROCESS of the <br> project. It is clear that <br> students are able to reflect <br> back and learn from doing <br> this project. | Students showed some <br> reflective thought. |  |  |
| Reflection <br> $\mathbf{2 ~ p t s ~}$ | Poster is not only a good <br> representation of this <br> project but is also <br> attractive, eye catching, <br> and easy to interpret. | Poster is attractive and <br> well thought out. May <br> not be as easy to <br> interpret. | Poster lacks thought <br> and attractiveness. <br> Difficult for audience to <br> get a clear picture of <br> the project. |  |
| Aesthetics <br> $\mathbf{2 ~ p t s ~}$ | Students go above and <br> beyond expectations with <br> either the worm bin or the <br> poster or both. |  |  |  |
| $\mathbf{2 ~ p t s ~}$ |  |  |  |  |




## Math

There is a lot of science in composting because the decomposition of the food and the life style of the worms and how the eat and work and digest and everything else they do are all part of biology. Biology is the study of living organisms and since there is basically only living things in the composter, it like a box o' biology. The nitrogen cycle happening through you the worms and there poop (compost) is like the way that they survive in the wild and how they normally live, with just less food because there are no humans in forests and things throwing there food scraps into the ground. Only other animals, but since they are survival animals they lave less.

Mari's garden gave us research and the inspiration


## Engineering the world

## Purpose

As you may know we are experiencing the rapid depletion of our resources. One of the things that is being wasted the most is our food supply. The solution to this problem is to get people to eat there vegetables even if I sound like your mom. If you have ever made or, grown your own food then you swear it tastes better so you eat it all. We are trying to make it so that every person can grow there own food more easily. Your worm composting bin was designed to be cool looking and work efficiently. We believe that if every body got one and every body started growing there food then we could be more efficient with your food system. Once we get our food system sorted I think that we can move on for the better.

the scale drawing

card board model



## Math

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## MPX WORM BIN PROJECT

## By Kris, Noah F, Isaiah P

n MPX we integrate math and science into our projects by using geometry and algebra in the calculations As you ff the cuts and the shapes angels, while also creating something which would improve sustainabilty in the
resourilassroom or at home
resouri
food $s$
there Ne started the worm bin project made ${ }^{2} y$ making scale drawings/ you ealculations of what we wanted grow tr)ur project to look like, then we designenade prototype boxes with
every:ardboard as to not waste more then wexpensive materials like wood get ol


After we assembled our prototypes we were ready to get to work building the real wood model. Some


We attached a handle and hinges and used glue/nails to connect all of the pieces


The only thing that we didn't anticipate was the length of the nail to the length of the wood, which looked like this until we got new, shorter nails


## MPX WORM BIN PROJECT

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1st Scale Drawing


2nd Scale Drawing


Final Product

After we failed on out first draft compost bin. We had to make the real thing. The 2nd scale drawing came after we made the final product, but it came out way better.

When we were making the first compost bin a problem was we approached the idea wrong. We started making little stacks and we could nave just made the sides and a cover. That made us build really fast so the problem was trying to make the correct angle. What we did was figure out the angles had to equal 135 degrees, but since it needs to be half of the 45 degree angle in half is 22.5 and that is the angle we needed to cut. After that was done it was east, we just connected the pieces with a screw and made the covers and lined the inside of it so the worms don't...

vere ready to get to work building the real wood model. Some red out while in cardboard form

and used glue/nails to connect all of the pieces


The only thing that we didn't anticipate was the length of the nail to the length of the wood, which looked like this until we got new, shorter nails

## HEXAGONS!

- HSG-GMD.A. 1 \& $2 \& 3$ APPLY GEOMETRIC CONCEPTS IN MODELING SITUATIONS
- HSG-CO.D. 13 MAKE GEOMETRIC CONSTRUCTIONS



## Hexagons \& Bees Infographic

## Teacher Name: Mr. Kaneko/Mr. Hines

| CATEGORY | 3 Mastery | 2 Developing | 1 Lacking | comments |
| :---: | :---: | :---: | :---: | :---: |
| Work Ethic | Individuals stayed on task nearly the whole time. Students worked hard. | Students stayed on task most of the time. There were occasional distractions, or re-directions required by the teacher | Students needed several redirections or were not actively involved. |  |
| Collaboration | Student clearly worked with other group members. Discussion of work and progress was clearly evident. | Student worked inconsistently with group. There was some evidence of more individual work. | Student needs to work on collaborating with others. |  |
| Biology/GeometryContent Why are bee hives Hexagonal? ( 5 pts) | Group addresses the issues including properties of a hexagon, distinguishing what a regular hexagon is from just a hexagon, the area formula, measure of interior angles and ho to construct one with a compass. Student brings additional information - what next or something interesting. <br> The poster should tie this Geometry info to bee hives and address the question of WHY they are hexagonal. | Group does not address one or two of the key ideas/comcepts in hexagons or treats the stated issues superficially. No "what next" included <br> Group does not address the question of WHY they form adequately or deeply. | Answer lacks clarity and does not answer question well. <br> Lacking in detail or may be missing important information in answering the question. |  |
| Graphics/Aesthetics | Elements of the content are nicely drawn, accurate and labeled properly. Plant Parts and the process of drawing a hexagon are told in a visually clear way. There is a balance between image and text and the infographic shows attention to detail, and is easy to read and pleases the eye. | Graphics may lack some detail or aesthetic quality. Might be missing some required steps, details or organisms. Material does not show real effort to lead viewer or be pleasing. | Graphics are lacking in detail and quality. Missing some important parts needed to properly explain this process. <br> Typos and messing markings distract form the message |  |
| Terms | Required terms are used IN EXPLANATION of hexagons and bees and not simply defined. | Either missing some terms, not properly used or simply defined. | Too few terms given for full credit. |  |





## THE

INTERCOOLER

- HSG-CO.A. $1 \& 3 \& 5$ EXPERIMENT WITH TRANSFORMATIO NS IN THE PLANE
- HSG-CO.D. 12 MAKE GEOMETRIC CONSTRUCTIONS


Cool as Ice
(adapted from nrich.maths.org)
Goal: To understand the different ways we can represent and build geometric solids
Essential Question: How do engineers construct 3-d models from 2-d materials?

## Activity 1: Triangle Construction with Compass

Essential Question: What are the properties that define a triangle and how can I draw them accurately?
Activity Instructions.
Teach yourself how to draw a triangle with a compass by following the instructions here:
http://wuw.mathopenref.com/consttrianglesss.htm
Once you feel you can draw triangles, play the following game*
Generate three random numbers from 1-10. Use the following website to generate your random numbers:
wow.random.org
Make sure to label the lengths of your triangle's legs. Do this until you have generated an assortment of triangles: Scalene, Right, Isosceles, Acute, Equilateral. What pattern do you see emerging? Can of triangles: Scalene, Right,

Once you have constructed your triangles, take a picture and post these on your posterous blog and explain what you learned from this activity.

If you want to construct a Right Triangle, you need to draw a right angle.
http:/hwow.mathopenref.com/constperplinepoint.html
Try to construct a few right triangles for practice!

## Activity 2: Understanding nets.

A net is a 2-dimensional representation that can be folded into a 3-dimensional shape.
Draw out the the sample net from the resources in iTunes U (labeled cube-net) and construct a cube from it. How many different nets can be designed to still build a cube? In your team see how many different nets you can create. You have 20 minutes to complete this activity.

What strategies to did you use to come up with your ideas? How many did you get?

Let's compare with other groups to see what they came up with.

## Activity 3: Cool as Ice challenge:

Intercoolers are used as a cooling mechanism, for instance for a car engine, by maximizing the airflow around the engine.

Your task is to design and construct a prototype intercooler, based on a cube, to house a model engine which requires cooling.
Intercooler Specifications
two opposing faces to be punctured by a diamond shaped hole in the center, which should be as large as possible without weakening the structure or allowing the 'engine' to fall out
the other two opposing faces to be punctured by 4 holes to take support tubes (drinking straws will be used in the prototype) the intercooler must support the engine when suspended by the support tubes

You have available to you:
$8.5 \times 11$ sheet of card stock (use this to construct your final product from a net of your design)


Scrap paper (for prototyping)
Compass
rulers, tape, pencils, scissors
4 drinking straws
1 model engine (teacher will have a model sample for the class)
Key questions you should consider before starting
What do you need to know/decide to complete this task?
What tasks will each group member have?
How will you make sure the coolers pass quality control

## Download taptap blocks





## WHITEBOARDS





## PREDICTIVE MODELING (POLYNOMIAL

 FUNCTIONS)- HSF-IF.B. $4 \& 5$ INTERPRET FUNCTIONS THAT ARISE IN TERMS OF THE CONTEXT
- HSF-IF.C. 7 ANALYZE FUNCTIONS USING DIFFERENT
REPRESENTATIONS
- HSF-BF.A. 1 BUILD A

FUNCTION THAT MODELS A RELATIONSHIP BETWEEN TWO QUANTITIES


## Predictive Modeling

Often in a physical system, we create a mathematical model to allow predictions to be made. Today we are gong to do just that.

1. Take the mechanical system from the teacher and place it at the edge of a table. Practice launching a ball from it.
2. Notice that the distance the ball travels horizontally is dependent on the angle that the arm on the device is swung.
3. Develop a plan to collect data so that a relationship (mathematical model) can be derived using Graphical Analysis between the angle and the diastase traveled
4. Run the experiment and develop the mathematical model. Take a couple of pictures of the experiment in action for later reference. Make sure to select the best model - be prepared to justify your rationale.
5. Once you have the model, let your teacher know - it is time to TEST your model to see if it can correctly predict a specific scenario!
6. For complete credit, you must send me your graphical analysis file (each team member needs to have their own) and a summary of results!


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| Angle <br> (degrees) | Trial 1 (cm) | Trial 2 (cm) | Trial 3 (cm) | Average <br> (cm) |
| ---: | ---: | ---: | ---: | ---: |
| 15 | 15 | 14 | 16 | 15 |
| 30 | 31 | 33 | 29 | 34.3 |
| 45 | 41 | 38 | 41 | 40 |
| 60 | 83 | 83 | 82 | 82.6 |
| 75 | 110 | 107 | 104 | 107 |
| 90 | 132 | 132 | 128 | 130.6 |

Mathematical Equation:
Distance $=.008\left(\right.$ degree) ${ }^{\wedge} 2+.795($ degree $)+.430$


```
84
    0=.008\mp@subsup{x}{}{2}+.795x-84.430
    b\pm\sqrt{}{\mp@subsup{b}{}{2}-4a}
x=-.795 \pm\sqrt{}{.79\mp@subsup{5}{}{2}-4(.008)(-84.450)}
x=\frac{-.795\pm1.82}{016}
x=\frac{1.025}{.016}}\quadx=64.0
```

(
sCALE MODELS: CATAPULTS COMMON CORE


Catapult Protypes:
Our goal today is to build a scale model of the catapult that we see on this page:
http://stormthecastle.com/catapult/mark-thomas-modified-ogre-catapult.htm
we will eventually make the actual model, but in order to see the construction requirements, a scale model is a good way to start.

## Schematic diagrams

to start, you are to make a three view schematic diagram so that you're both aware of the materials needed, as well as how they fit together and other design considerations. On one piece of graph paper, accurately and completely create top, side, and front view diagrams making sure to include all important measurements and edges, drawn accurately and with straight lines using a ruler and labeling all parts as necessary.
please look at these presentations about how to make a scale drawing:
http://www.authorstream.com/Presentation/Tirone-38765-Orthographic-Projection-Multi-View-Drawing-History-Revolving-pr-Education-ppt-powerpoint/
http://www.authorstream.com/Presentation/waqqas-314623-orthographic-projection-education-ppt-powerpoint/

Here are a few examples of what a good three view representation should look like:
http://image.thefabricator.com/a/articles/images/2249/precision-large-view-figure5b.gif
http://www.dimcax.com/gdt web/november-04 files/july-02-1.gif
http://upload.wikimedia.org/wikipedia/commons/thumb/4/45/Mech_draw_1.svg/200pxMech draw 1.svg.png
http://graphicalcommunication.skola.edu.mt/wp-content/uploads/2010/09/Engineering-Drawing-1.jpg
http://engineeringtraining.tpub.com/14069/img/14069 162 6.jpg
http://graphicalcommunication.skola.edu.mt/wp-content/uploads/2010/09/Form-4-HYE-2009-010109-Model-11.jpg

Once you have created your schematic orthographic drawings and have them approved, get your materials and build a $1 / 4$ scale model of the catapult.



## MODELING ACCELERATED MOTION

- HSA-CED.A. $1 \& 2$ CREATE EQUATIONS THAT DESCRIBE NUMBERS OF RELATIONSHIPS
- HSF-BF.A. 1 BUILD A FUNCTION THAT MODELS A RELATIONSHIP BETWEEN TWO QUANTITIES



## Modeling Motion

In this activity, we are going to run an experiment in which an object rolls down an incline plane, and we examine the relationship between how far it rolls, and how much time it takes.

In order to set up this activity, you will use your iPad both as a camera, timer, and mathematical analysis tool. we will discuss the particulars of the experiment design as a class, but the outcome should be a document that includes the following:

- brief description of the experiment with a picture of the experimental setup
- data table that includes multiple trials, and averages
- graph of data that includes appropriate choice in mathematical model and appropriate
use of labeling axes and fit
- a mathematical model stated (equation) using correct variables and units on any constants
- a written statement of the relationship of the variables
- a brief discussion of experimental questions and concerns
this should be submitted as a PDF document in this week's Showbie folder

Resources supporting this activity
http://www.youtube.com/watch?v=ZUgYc6Bi46w
http://demonstrations.wolfram.com/GalileosInclinedPlaneExperiment/
http://www.youtube.com/watch?v=tUmVqgBp06s
http://www.youtube.com/watch?v=qBAh2zN7se4



In the lab which we conducted we timed the amount of seconds it took for a car to reach the end of a rial. We recorded it with video. We had one person taping, one person start/stop the timer and start the car, and one person stop the car. We then used the recorded data to construct charts, tables, and functions.

$\mathrm{D}=$ distance in cm
$\mathrm{T}=$ time in seconds
$D=72.9 \mathrm{~T}^{\wedge} 2+(-51.2) \mathrm{T}+33.2$

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$\mathrm{D}=$ distance in cm
$\mathrm{T}=$ time in seconds
$D=72.9 T^{\wedge} 2+(-51.2) T+33.2$

Graph:


This graph is using a quadratic formula. The equation given is $\mathrm{y}=\mathrm{ax}$ squared + $\mathrm{bx}+\mathrm{c}$. So to take this equation and make it so that it is specifically fitting this set of data we must change the letters used. So the equation would read: $T$ (time)=
ad (distance)squared $+\mathrm{bd}+\mathrm{c}$. Then when you plug in the numbers it would be $\mathrm{T}=$ 3.704 d squared $+.002 \mathrm{~d}+.354$. We chose this style of graph because of how well it fit the plotted points that were on the graph.


This is an image of the set up we used to perform this experiment. Shows the ramp, the pieces of blue tape, object rolling down, timer set up next to the ramp, and the people at both ends.

## EXPLORING MATH PATTERNS IN ART

- HSA-REI.A. 2 REPRESENT AND SOLVE EQUATIONS AND INEQUALITIES GRAPHICALLY
- HSA-REI.D. 11 REPRESENT AND SOLVE EQUATIONS AND INEQUALITIES GRAPHICALLY
- HSA-CED.A. 3 CREATE EQUATIONS THAT DESCRIBE NUMBERS OR
RELATIONSHIPS



## Exploring Math Functions and Inequalities Through Art

In this activity, we're going to explore ways in which some forms of art can be re-expressed as mathematical functions, and developed an original piece of art that you will create a mathematical function for.

This activity explores the Algebra 2 topics of functions, equations and graphs, as well as Linear systems including any qualities. it also begins to explore some of the functional relationships covered later in the course that include quadratics, radical expressions, and other functional forms that create different kinds of curves.

## Step 1: Bitmap vs Vector graphics

One of the important basic concepts to understand in the marriage between arts and digital technology is the difference between bitmap (painting or raster) graphics and vector graphics. There are a variety of software and mobile applications for both kinds of graphics. start by reading and understanding the difference between them at this link, and explore this a little on your own Web search before you continue:
httolloraphicssoft about.com/od/aboutgraphics/a/bitmapvector-htm
Make sure you understand the difference and can explain this, since it is a critical idea in this activity.

## Step 2: Exploration of Geometric centered art

graphic art and painting covers a wide range of style and historical approaches, but there are a few that lend themselves easily to creating mathematically-based (vector) descriptions. A few examples of styles include:

- Cubism
- Mondrian
- Albers
- Kandinsky

All of these approaches have in inherently visual mathematical structure that can be easily unfoided. Using a web browser, learn more about each of these styles, and look at a variety of images of each of these arts styles. For each of the four listed, pick three images that you think are interesting and convey a geometric sense of wholeness. Keep track of these images by putting them into your photo library so you can include them in a summary document during this activity (make sure to keep the URL, so you can give correct reference of where you got it).
In your own words, give a paragraph description of each style, and your three examples using a word processor Ike Pages, and put this document in our class digtal dropbox for this activity. Your goal will be to create a piece of art modeled after one of these styles. Please indicate at the end of your summary which style you would like to mimic, and why. Don't forget to add references/iinks/urls for both your images and your research! Checklist for submission here

## Step 3: First Draft

Using just pencil and an $81 / 2 \times 11$ sheet of paper, create a sketch of your intended piece of art - no color necessary at this point. be sure to think about your use of line and curve, as every line in curve you draw will need to be modeled using the software Desmos.
Once you have completed this first draft, take a picture of it with your iPad in put it in your showbie folder we will do a round of critiquing and feedback as a class.

Step 4: Revision and Color
Taking into account the feedback that we collected as a class, go back to your original draft, and now strengthen your lines and curves, and add color to bring your sketch to life. once you are finished, take a picture of this, and put that image in your dropbox.

Step 4: Croating the Mathematical Model
In order to convert your drawing into a digital mathematical model, we need to create a coordinate system with your drawing so that we can convert lines and curves into mathematical statements that match up to a coordinate plane. Although there are a variety of ways we could accomplish this, a simple physical way would be to put a transparent grid on top of your drawing, and start mapping the points where lines and curves begin and end (think domain and range of each function) and then defning the mathematical statements for each one of those lines and curves. For each type of geometric shape, there is a corresponding relationship (function) that will best fit your drawing. In class, we discussed and played with a variety of functions that correspond to the conic sections that are central to so much of the work in algebra 2: line, circle, parabola, elipse. Hyperbola.
These can easily be found by web searching but there is one example of their mathematical statements here: htto:/hwwwwyzant.com/help/math/algebralconic_sections

You can also look at examples on the Desmos website (http://desmos.com) to see examples of other projects and the curves that were made and what mathematical statements allowed them - please remember you'll need to consider limitations of domain and range for your functions.

## Deliverables and assessments:

- Fluency with understanding bitmap and vector graphics (this will be quizzed at some point)
- Summary of your exploration of the different kinds of art submitted as a PDF in our digital dropbox from step two. Checklist for completion here
- First draft submitted in digital dropbox
- Second draft submitted in digital dropbox



## Student Name:

## Art in Math Project (43 pts):

- Top of reflection page includes student name and project tite (1 pt)


## - Prolessional Level of Work ( 2 pts .):

Ois work free of tyos misspeliod words. and, punctuation and grammatical errors? Qis work free of typos, misspeliod Comments

## Art work ineluded (12 pts.): <br> WWas the artwork included?

Gooes the artwork to indicate attenton to detail
Are there ciean ines, appropriate coloring and shading, attertion to detai? Comments: Comments:

- Desmos Printout included (12 pts.):
ØWas a printout included?

ODoes the pritt out have both the graphs as wel as all of the functions?
OAre domain and range imits clearly used?
ZAre the functions writer with accepted mathernatical clarity?
When appropriate, are the representations of ines, and other conic sections?
Oys there use of inequalities?
Qooes the use of functions indicate attention to detal in lines matching up and shading from inequalites that is consistert with the overal drawing? Cormments:

```
- Organization of Reflection (2 pts.):
Ols the wring at an appropriate level?
Ois it organized in a clear and logical marner?
Is it clesr, concise, and free of redundancies and extra wording?
Is it "reader criemed," that is pleasant and easy 10 read?
commont:
Cormments:
```

```
- Reflection Content (s pts.):
Qis there a clear explanation of how the artwork is dram in the style of a particular artist? Oooes that detail include description of objects, function and form, color and balance
QAre there spocific examples given within the text?
OAre at least throe spocific tunctions in the Desmos printout dsoussed inciuding thei form and tunction within the graph?
पAre domain and range imits discussed?
Qls there mertion of conic sections and an explanation of their functions representation?
Qls there a discussion of inequalites and how they are shom in the project?
Ois there a recognition of permutations (translation) of the functions?
Ois there discussion of the challenges and successes?
OAre specific examples given?
Commere guidance given to the viewer that leads them to appreciate aspects of your work? Corments:
```


$y=-2.2 x-98\{-56<x<-51.9\}$
$x=-1 y-32(-45<x<-42)$
$x=5 y-110\{-45<x<-41.5\}$
$y=9 x+389\{-42.12<x<-41.7\}$
$x=-38.4\{-4.2<y<4.2\}$
$x=-1.9 y-31\{-38.5<x<-32\}$
$x=1.2 y-33\{-38.4<x<-32.1\}$
$y=-16.3\{-59.9<x<-51.9\}$
$y=2.2 x+98\{-56<x<-51.9\}$
$y=-2.2 x-148\{-59.89<x<-55.9\}$
$x=-71.3\{-4.2<y<4.2\}$
$y=-.5 x-39.7\{-79<x<-71.3\}$
28. $y=5.5 x+40\{-79<x<-71.3\}$
2. $y=1 x+31\{-13<y<-10\}$
30. $x=20 \sin (.08 y+5)-38\{-14<y<2\}$
$x=10 \sin (.15 y+5)-38\{2<y<6.5\}-10$
2. $x=10 \sin (.3 y+5)-38\{10<y<14\}-23$



44]


Desmes Autection


While preparing for my At and Math project I researched a series of artets and gente of art Two that stood out were Mondrian and Kandinsty: skinniar rectanglos. They alf up completelely dr rectangles Longer, shother tumer, and is not repetive but mix match. He also uses primary or basic colors to complesty in (2)

Kandinsky is psychedolic. He uses al types of shaces and colors to create a mind
bending experience. His art explodes of the canvas. He uens mato and bending experience. His art exploses of the canvas. He uses coloc, shape, size, and brightoess all at once to triy surprise his audence. I love his artwork and it is truly a
masteppece. Kandinsky ues a bef more stupes. Iines and stratums to git mastiety and action.
theer ike thad a lot of successes and challenges both which I overcame and wasn drawing a similar att work to the ingsiring peject. Ifeel I had a lot of fun and success in drawing a similar art work to the inspiring pieces. I also feel it was a lot easier because only used crcle and line equations. it was very hard though to draw the circles on rough it out. Also that desmos only has a wanted to make it precise. So I just had to because I couldnt do a lot of ant related hastricted amount of colors was annoying
a great time croating, editing, and being inspired by art end math.



## FORM AND FUNCTION IN THE REAL WORLD: QUADRATICS

- HSA-SSE.A. 1 INTERPRET THE STRUCTURE OF EXPRESSIONS
- HSA-APR.B. 3 UNDERSTAND THE RELATIONSHIP BETWEEN ZEROS AND FACTORS OF POLYNOMIALS
- HSA-CED.A. 3 CREATE EQUATIONS THAT DESCRIBE NUMBERS OR RELATIONSHIPS
- HSF-BF.B. 3 BUILD NEW FUNCTIONS FROM EXISTING FUNCTIONS



Above is my real life Porabola

Your goal today is to find a shape in the real world outside the classroom that looks parabolic, and to develop the mathematical function that reprints it.

Step 1: Take your iPad and go outside with a partner and find some natural or man made object that takes the form of a parabola. Take a picture of that object (maybe take a couple just to make sure)

Step 2. Back in the class room, take your picture and align it so that it is either opening upward or downward. Zoom in so it fills the screen. Place a grid on top of the shape. Define where the origin is (do not put it on the vertex of your parabola).

Step 3: Find a least three points on the parabola from your grid - make sure the write these down

Step 4: We know the standard form of a parabola is $Y=A x^{\wedge} 2+B x+C$. Since you have at least 3 pairs of $X$ and $Y$ values, you can plug these into the standard form to create an equation of $A$, $B$ band $C$. For example if one of your points was $(2,-3)$, it would be
$Y=A x^{\wedge} 2+B x+C$
$-3=A(2)^{\wedge} 2+B(2)+C$
$-3=4 A+2 B+C$
Step 5: Now that you have 3 equations with 3 unknowns, you can use either substitution, elimination or matrix to solve the 3 equations to find the values of $A, B$ and $C$. There is a way to use your graphing calculator to solve it through matrices - here is one explanation:
http://www.youtube.com/watch?v=FILsxIWD6a8
here is another
http://www.missouriwestern.edu/cas/documents/MatricesonTl2013.pdf

Step 6: Once you have solved for A, B and C write the function and graph it using Desmos. Does it look like the curve you saw in nature?

Step 7: Trace the curve from Desmos onto a transparency sheet. Overlay the curve onto your original picture - does it match?

Step 8: Summarize! For your reflection, type up a summary that includes your original picture, your math work (points, description of you three equations, how you solved them), your overlay (capture this somehow), and a summary of how well your function fit your form. Pau.

Step 9: BONUS! Every Quadratic Function can be written in standard form


## SOME FINAL THOUGHTS

- Lots of good resources out there to get started (see Bibliography)
- Problems come from the real world - think like a mathematician! Or at least Dan Meyer (water fountain, draining pool)
- Celebrate Student work - make excellent work visible
- time time time!
- partner with/befriend a science teacher



## BIBLIOGRAPHY \& RESOURCES

- Bryan Meyer: Doing Mathematics http://www.doingmathematics.com
- Dan Meyer http://blog.mrmeyer.com
- Buck Institute for Education http://bie.org
- Envision Learning Project exchange: http://www.envisionprojects.org/cs/envision/ print/docs/750
- High Tech High Math Resources: https://sites.google.com/a/hightechhigh.org/hth-math-common-core-standards/home
- ASU Modeling: http://modeling.asu.edu
- PERTS: http://www.perts.net/home/orientation/cp2.php
- Vernier http://www.vernier.com
- Makerspace: http://makerspace.com


## About MPX

MPX Program is an innovative, interdisciplinary program featuring a project-based curriculum as the primary focus of student work. This curriculum encourages students to synthesize their knowledge of Language Arts, Social Studies, Science, and Engineering through participation in collaborative "real world problem solving" setting. This school year we have projects addressing sustainability including auditing the energy use of each building on this campus that will be used to address the school's carbon footprint, and designing and constructing urban garden systems that will be used to grow produce for a cook-off competition.

On the right side of this page, you see a series of links to other activities we have done as well as links to blogs that give you a up-to-date view of the work our leaders and learners are doing - challenges and successes, their reflections about their work and the process involved in rolling up our sleeves and trying to do authentic problem-solving.

We hope you will take time to explore the activities our learners have been immersed in. If you have an interest in being involved with our program as a resource, or have questions, please contact mpx@midpac.edu

Imual (onward!)

MID-PACIFIC INSTITUTE EXPLORATORY NEWS
Nov On Math, Modeling and Applied learning

## Explore MPX

- MPX Home
- More about MPX
- MPX Frequently Asked Questions
- An Overview of MPX [.pdf]


## MPX Teacher Blogs

© Heather Calabro's MPX 9 Humanities Blog
(-) Mark Hines' MPX 10 STEM blog
(-) Gregg Kaneko's MPX 9 STEM blog

- Laura Davis' MPX 10 Humanities blog


## Videos/Documents

- MPX by MPX'ers
(-) Kolea Farms Field Trip
( $)$ Visual Mapping
(-) What is MPX? In student voice from their presentations of learning Fall 2011


THE SLIDES THAT FOLLOW WERE NOT PART OF THE PRESENTATION BUT INCLUDED AS ADDITIONAL RESOURCES FROM OTHER PROJECTS

## Working with Notability

## Exercises

Solve each equation. Check for extraneous solutions.
27. $|2 x+8|=3 x+7^{2}+\cdots$

29. $3|x+10|=6$

30. $2|x-7|=x-8$

Solve each inequality. Graph the solution.
31. $|3 x-2|+4 \leq 7$
32. $\left.4 \frac{\mid y-9}{4} \right\rvert\,>\frac{36}{4}$

33. $|7 x|+3 \leq 21$

34. $\frac{\frac{1}{2}|x+2|}{1 / 2}>\frac{6}{1 / 2}$ $\qquad$



## EXAMPLE: AQUAPONICS PROJECT

Aquaponics Kickstarter Proj
This page will host all of our resources for this project

Fubrics. Todo lists, descriptions, elc

Team Roles and Responsibilities:

## (x) Team roles kickstarter.pages

Team To-Do List - to be downloaded by each Contractor and shared with team members, me, Hines and Kaneko:
(-5) Team Task Sheet.tumbers


Students as:
Designers, Builders, Salesman, Scientists, Reflective Writers,
Social Media Advocates

## Scaffolded Design:

Essential Question, Clear timeline and deliverables, roles and responsibilities, voice and choice, use of technology

MPX9 Spring 2013


Krislyn's Team
03/08/2013
Contracter (Krislyn):
The process of creating our aquapooic system was hard for me to manage. It was hard to get a read on my group beccuise at ons point their minds eev entirsty focused on whet they are doing, then all of a sudden they become unmotivated. To help get my group on task agalh, I needed to be more firm with them. I used to yell at them at one
 Ine again in the beginning of this project, we wec awars betind che ches all te idess $=$ hem had decided which one would be better and what model would actually function the best Second, our prototypes were the lat to be completed due to the lack of time we had deciding whet ides to ute. The one thing I could reviy on my group was getting the job done. I felh that even though our strategles were off and on, we were able to get through all the

Author
Write somathing about yourself. No need to be lancy, just an awerview.

## Archives

## TECHNOLOGY IN THE SERVICE OF LEARNING



| \NTRD: OUR LDGO LWHAT AQUAPONcs is. <br> $2^{\text {nd }}$ Plcture process dsteps of how be built oursystem <br> 5" picture: Pi-ch (why you should bry our slstem complied to other ones VIDEO(PITCH) <br> - FINISHED PROTVCT (PICTURE) <br> - Closina summary <br> - summany of why this is more efficiert <br> - picture of jur finished product |
| :---: |
|  |  |
|  |  |
|  |  |




## The Water Fountain

Take a look at the pictures below. This is of one of the many water fountains you see on our campus. You can also see that it is plugged in, which means it is using a small air-conditioning unit to cool off water that you drink. How much electricity is it using to do this? And how much does it cost to run this over the course of a year?

The second photograph shows the information from the unit - notice that it uses 5 A at 115 V .

## Calculation 1:

If this unit were running continuously, how much energy would use? How much would it cost to run it for one calendar year assuming it is plugged in continuously if electricity costs $\$ .34$ a kilowatt hour?
( You might remember that the power device uses is the product of voltage and current $\mathrm{P}=\mathrm{VI}$ )
but wait - here's another way to view the problem:

## Calculation 2:

A watt meter was plugged into the unit in the following data was gathered:
Length of time watt meter was plugged in: two hours and 47 minutes (2:47)
Kilowatt hours consumed during that time period: 0.14 kWHr
If this is the typical power use based on the data above, recalculate and figure out how much it would cost to run this device for a calendar year nonstop.

## Reflect:

How do your two values in calculation $1 \& 2$ compare? Explain any discrepancies.


